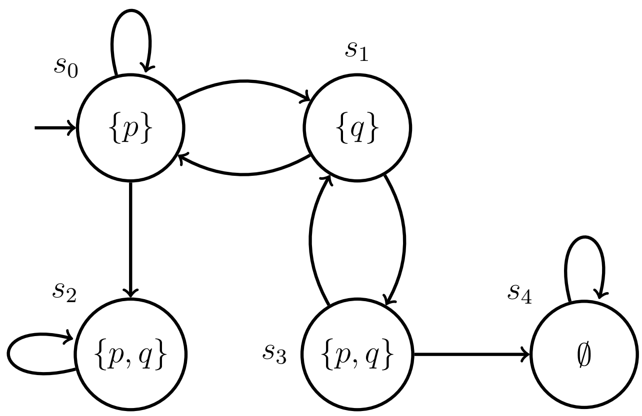
Model Checking – Exercise sheet 7

Exercise 7.1
Compute $[\![\mathbf{EG}q]\!]$, $[\![\mathbf{EXAG}(p \vee q)]\!]$ and $[\![\mathbf{EFAG}(p \wedge q)]\!]$ for the following Kripke structure:



Exercise 7.2
(Taken from *Principles of Model Checking*)
Provide two Kripke structures $\mathcal{K}_1$ and $\mathcal{K}_2$ (over the same set of atomic propositions) and a CTL formula ϕ such that $Traces(\mathcal{K}_1) = Traces(\mathcal{K}_2)$ and $\mathcal{K}_1 \models \phi$, but $\mathcal{K}_2 \not\models \phi$.

Exercise 7.3
Given two CTL formulas ϕ_1 and ϕ_2, we write $\phi_1 \Rightarrow \phi_2$ iff for every Kripke structure $\mathcal{K}$ we have $(\mathcal{K} \models \phi_1) \Rightarrow (\mathcal{K} \models \phi_2)$. Furthermore, we define an *implication graph* as a directed graph whose nodes are CTL formulas, and that contains an edge from ϕ_1 to ϕ_2 iff $\phi_1 \Rightarrow \phi_2$. Let $AP = \{p\}$.

(a) Draw an implication graph with the nodes: $\mathbf{EFEF}p$, $\mathbf{EGEG}p$, $\mathbf{AFAF}p$, $\mathbf{AGAG}p$.

(b) For each implication $\phi_1 \Rightarrow \phi_2$ obtained in (a), give a Kripke structure $\mathcal{K}$ that satisfies ϕ_2 but not ϕ_1, i.e. give a $\mathcal{K}$ such that $\mathcal{K} \models \phi_2$ and $\mathcal{K} \not\models \phi_1$.

(c) Add the following CTL formulas to the implication graph obtained in (a): $\mathbf{AFEF}p$, $\mathbf{EFAF}p$, $\mathbf{AGEG}p$, $\mathbf{EGAG}p$.