

## Model Checking – Exercise sheet 8

### Exercise 8.1

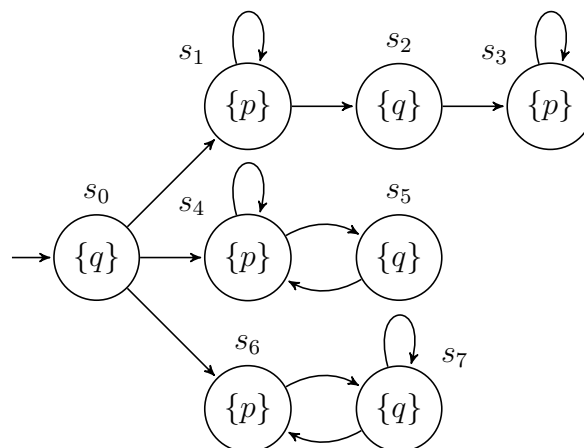
Given two CTL formulas  $\phi_1$  and  $\phi_2$ , we write  $\phi_1 \Rightarrow \phi_2$  iff for every Kripke structure  $\mathcal{K}$  we have  $(\mathcal{K} \models \phi_1) \Rightarrow (\mathcal{K} \models \phi_2)$ . Furthermore, we define an implication graph as a directed graph in which nodes are CTL formulas and there is an edge from  $\phi_1$  to  $\phi_2$  iff  $\phi_1 \Rightarrow \phi_2$ .

Let  $AP = \{p\}$ .

- Draw an implication graph with the nodes: **EF EF p**, **EG EG p**, **AF AF p**, **AG AG p**.
- Add to the graph in (a) the following CTL formulas: **AF EF p**, **EF AF p**, **AG EG p**, **EG AG p**.
- For each implication  $\phi_1 \Rightarrow \phi_2$  in (b), give a Kripke structure  $\mathcal{K}$  that only satisfies  $\phi_2$  but not  $\phi_1$ , i.e. give a  $\mathcal{K}$  such that  $\mathcal{K} \models \phi_2$  but  $\mathcal{K} \not\models \phi_1$ .
- Complete the graph in (b) with the nodes: **AG AF p**, **AF AG p**, **AG EF p**, **EG AF p**, **AF EG p**, **EF AG p**, **EF EG p**, **EG EF p**.

### Exercise 8.2

Consider the following Kripke structure over  $AP = \{p, q\}$ :



- Compute  $\llbracket \mathbf{EG} q \rrbracket$  and  $\llbracket \mathbf{EF} q \rrbracket$ .
- Compute  $\llbracket \mathbf{AG} \mathbf{AF} p \rrbracket$  and  $\llbracket \mathbf{AF} \mathbf{AG} p \rrbracket$ .